NMR-like Control of a Quantum Bit Superconducting Circuit

E. Collin, G. Ithier, A. Aassime, P. Joyez, D. Vion, and D. Esteve

Quantronics group, Service de Physique de l’Etat Condensé, DSM/DRECAM, CEA Saclay, 91191 Gif-sur-Yvette, France

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Coherent superpositions of quantum states have already been demonstrated in different superconducting circuits based on Josephson junctions. These circuits are now considered for implementing quantum bits. We report on experiments in which the state of a qubit circuit, the quantronium, is efficiently manipulated using methods inspired from nuclear magnetic resonance (NMR): multipulse sequences are used to perform arbitrary operations, to improve their accuracy, and to fight decoherence.

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Despite progress in the development of quantum bit (qubit) electronic circuits, the complexity and robustness of the operations that have been performed on them are presently still too primitive for demonstrating quantum computing (QC) [1]. Presently, the most advanced qubit circuits are superconducting ones based on Josephson junctions. The preparation of coherent superpositions of the two states of a qubit has already been demonstrated for several circuits [2–9], and a two qubit gate was operated [10]. However, qubit operations are far less developed for qubit circuits than for atoms or spins. In this Letter, we report on experiments that successfully manipulate a Josephson qubit based on the quantronium circuit [11], using NMR methods. We demonstrate that any transformation of the qubit can be implemented, that they can be made robust, and that decoherence can be fought. Note that using NMR methods for qubit manipulation does not bring in the intrinsic limitations of QC with nuclear spins, such as the lack of scalability, because in this approach the NMR sequence is applied to a single distinguishable qubit, not to an ensemble.

The quantronium circuit, described in Fig. 1, is derived from the Cooper pair box [12,13]. It consists of a superconducting loop interrupted by two adjacent small Josephson tunnel junctions with Josephson energy \( E_J/2 \) each, and by a larger Josephson junction (\( E_{J0} \approx 15E_J \)) for readout. The island between the small junctions, with total capacitance \( C_\Sigma \) and charging energy \( E_C = (2e)^2/2C_\Sigma \), is biased by a voltage source \( U \) through a gate capacitance \( C_g \). The characteristic energies measured in the present sample are \( E_J = 0.87k_B \) K and \( E_C = 0.66k_B \) K. Experiments are performed at 20 mK using filtered lines. The eigenstates of this system are determined by the dimensionless gate charge \( N_g = C_gU/2e \), and by the superconducting phase \( \phi = \gamma + \phi_0 \) across the two small junctions, where \( \gamma \) is the phase across the large junction and \( \phi = \Phi/\Phi_0 \), with \( \Phi \) the external flux through the loop and \( \Phi_0 = h/2e \). The two lowest energy states \(|0\rangle \) and \(|1\rangle \) form a two-level system suitable for a qubit. At the optimal working point (\( \delta = N_g = 1/2 \)), the transition frequency \( \nu_{01} \) is stationary with respect to changes in the control parameters, which makes the quantronium insensitive to noise at first order [3,11]. For the sample investigated, \( \nu_{01} = 16.40 \) GHz at the optimal working point. For readout, \(|0\rangle \) and \(|1\rangle \) are discriminated through the difference in their supercurrents in the loop [3]. A trapezoidal readout pulse \( I_b(t) \) with a peak value slightly below...
the critical current \( I_0 = E_{R0}/\varphi_0 \approx 450 \text{ nA} \) is applied so that the switching of the large junction to a finite voltage state is induced with a large probability \( p_1 \) for state \(|1\rangle\) and with a small probability \( p_0 \) for state \(|0\rangle\). The switching is detected by measuring the voltage across the readout junction, and \( p \) is determined by repeating the experiment a few \( 10^4 \) times. The fidelity \( \eta \) of the measurement is the largest achieved value of \( p_1 - p_0 \).

The manipulation of the qubit state is achieved by applying time dependent control parameters \( N_g(t) \) and \( I_p(t) \). When a nearly resonant microwave modulation \( \Delta N_g \cos(2\pi \nu_{\text{RF}} t + \chi) \) is applied to the gate, the Hamiltonian described in a frame rotating at the microwave frequency \( \hbar = -\hat{H} \cdot \hat{\sigma}/2 \) is that of a spin \( 1/2 \) in an effective magnetic field \( \hat{H} = \hbar \Delta \nu \hat{z} + \hbar \nu_{\text{RF}} \hat{x} \cos \chi + \hat{y} \sin \chi \), where \( \Delta \nu = \nu_{\mu\mu} - \nu_{01} \) is the detuning, and \( \nu_{\text{RF}} = 2E_c \Delta N_g (\langle 1|\hat{N}|0\rangle)/\hbar \) the Rabi frequency. At \( \Delta \nu = 0 \), Rabi precession takes place around an axis lying in the equatorial plane, at an angle \( \chi \) with respect to the \( X \) axis. Rabi precession induces oscillations of the switching probability \( p \) with the pulse duration \(|3\rangle\). The range of Rabi frequencies \( \nu_{\text{RF}} \) that could be explored extends above 250 MHz, and the shortest \( \pi \) pulse duration for preparing \(|1\rangle\) starting from \(|0\rangle\) was less than 2 ns. The fidelity was \( \eta = 0.3-0.4 \) for readout pulses with 100 ns duration at the optimal value of \( \delta \) at readout. This fidelity might be improved using rf methods that avoid switching to the voltage state \(|4\rangle\).

In order to perform arbitrary operations on the qubit, one has to combine rotations around different axes \(|1\rangle\), i.e., pulses with different phases. For that purpose, a continuous microwave signal is divided on two lines, one being phase shifted as desired. Both lines are led to mixers controlled by dc pulses, and then recombined and applied to the gate. In Fig. 2, measurements of the switching probability \( p \) following two-pulse sequences combining \( \pi/2 \) rotations around the axes \( X, Y, -X, \) or \(-Y \), are shown. Theory predicts that \( p \) oscillates at frequency \( \Delta \nu \) with the delay \( \Delta \tau \) between pulses. This experiment is analogous to the Ramsey experiment in atomic physics, and to the free induction decay in NMR. When the two pulses have different phases \( \chi_1 \) and \( \chi_2 \), the Ramsey pattern is phase-shifted by \( \chi_2 - \chi_1 \). Despite the presence of spurious frequency jumps due to individual charge fluctuators near the island, the overall agreement for the phase shift of the Ramsey pattern demonstrates that rotations around axes \( X \) and \( Y \) combine as predicted. Arbitrary unitary transformations can thus be performed. Rotations around the \( Z \) axis can, however, be more readily performed by changing the qubit frequency for a short time. A triangular bias-current pulse with maximum amplitude \( \Delta I \) is applied in a Ramsey experiment. During this detuning pulse, a phase difference \( \zeta = 2\pi \int \delta \nu_0(t) dt \) builds up between the qubit states, which is equivalent to a rotation around the \( Z \) axis with an angle \( \zeta \). The Ramsey pattern is phase-shifted by \( \zeta \) as shown by the oscillations of \( p \) with \( \Delta I \) (right panel of Fig. 3).

The accuracy and robustness of these qubit operations are also important issues. In NMR, composite pulse methods have been developed to make such manipulations less sensitive to rf pulse imperfections \(|5,6\rangle\). In the case of the CORPSE sequence (compensation for off-resonance with a pulse sequence), the sensitivity to de-
tuning is strongly reduced, the error starting at fourth order. We have tested this sequence in the case of a $\pi$ rotation around the $X$ axis, which performs a NOT operation on the qubit. The corresponding CORPSE $\pi(X)$ pulse sequence is $\{7\pi/3(X), 5\pi/3(-X), \pi/3(X)\}$ [15]. As shown in Fig. 4, it is significantly more robust against detuning than a single pulse $\pi(X)$ since the switching probability stays close to its maximum value over a larger frequency range, comparable to the Rabi frequency. By performing the CORPSE sequence after an arbitrary rotation $\theta(-X)$, we have also checked that the sequence works for a general initial state.

Another major concern of qubit circuits is to improve quantum coherence, which is limited by relaxation and dephasing. The relaxation time $T_1$ was 500 ± 50 ns at the optimal working point. The lifetime of coherent superpositions is given by the decay of the Ramsey oscillations. This decay was close to exponential with $T_2 = 300 ± 50$ ns for the present sample at the optimal working point (see top panel of Fig. 5), showing that dephasing dominates decoherence. $T_2$ becomes progressively shorter when the working point is moved away [3]. NMR concepts are again useful for fighting decoherence. First, the well known spin-echo technique [17] suppresses the effect of slow variations of the qubit frequency [5]. By inserting a $\pi$ pulse in the middle of a Ramsey sequence, the random phases accumulated during the two free evolution periods before and after the $\pi$ pulse cancel provided that the perturbation is almost static on the time scale of the sequence. The echo method thus provides a simplified form of error correction between an initial and a final one. As shown in Fig. 5 (middle panel), we have recorded echoes, and the echo minimum at the nominal echo position as a function of the total sequence duration. The small residual oscillations on the echo minimum result from the finite duration of the pulses and from a slight residual detuning, and simulations taking these effects into account, show that the echo decay time $T_E$ is the decay time of the envelope of these oscillations. At the optimal point, we find $T_E = 550 ± 50$ ns $\sim 2T_2$, which agrees with the prediction for the second order contribution of the charge noise, propor-

![FIG. 4. Demonstration of the robustness of a composite pulse with respect to frequency detuning: switching probability after a CORPSE $\pi(X)$ sequence (disks), and after a single $\pi(X)$ pulse (circles). The dashed line is the prediction for the CORPSE, and the arrow indicates the qubit transition frequency. The CORPSE sequence works over a larger frequency range. The Rabi frequency was 92 MHz. Inset: oscillations of the switching probability after a single pulse $\theta(-X)$ followed (disks) or not (circles) by a CORPSE $\pi(X)$ pulse. The patterns are phase shifted by $\pi$ as predicted.](image-url)

![FIG. 5. Top panel: switching probability (dots) after a Ramsey $\{\pi/2(X), \pi/2(X)\}$ sequence at $\Delta \nu = +50$ MHz, as a function of the time delay between pulses. The lines are exponential fits of the envelope with a time constant $T_2 = 350$ ns. Middle panel: example of echo measured with a $\{\pi/2(X), \pi(X), \pi/2(X)\}$ sequence by increasing only the delay between the first $\pi/2$ and the $\pi$ pulses (dots). The arrow indicates the nominal position of the echo minimum. Thin line: echo signal at the nominal minimum position, obtained by increasing the total sequence duration, while keeping the $\pi$ pulse precisely in the middle. The bold line is an exponential fit of the envelope with a 550 ns time constant. The dashed line shows a fit of the lower envelope of the Ramsey pattern measured in the same conditions (220 ns time constant). Bottom panel: switching probability (thin lines) after two spin-locking sequences with a Rabi locking frequency of 24 MHz, at the optimal working point, versus sequence duration. Thick lines: exponential fits of the envelopes, with time constant 650 ns (see text). The dashed lines show a fit of the envelope of the Ramsey pattern measured in the same conditions (time constant: 320 ns).](image-url)
yields due to finite pulse length and detuning. The envelope Lock the signals after the two spin-locking sequences frequency. The bottom panel of Fig. 5 shows the decay of occur under the effect of fluctuations at the Rabi locking evolves in time. Depolarization of the states Hamiltonian in the rotating frame, and only its phase prepared by the first pulse is thus an eigenstate of the superposition is recovered only once per Rabi period, By encoding in the rotating frame a coherent superposition densities in the range \((2–100 \text{ MHz})\) (data not shown). By encoding in the rotating frame a coherent superposition of the eigenstates, decoherence is fought, but the superposition is recovered only once per Rabi period, with an effective coherence time \(T_2 > T_1\).

In conclusion, we have demonstrated that the state of a quantumonium qubit can be efficiently manipulated using methods inspired from NMR. Rotations on the Bloch sphere around \(X\) and \(Y\) axes have been performed with microwave pulses and combined, rotations around \(Z\) have been done with adiabatic pulses, and robust rotations have been implemented using composite pulses. Finally, the spin-echo and spin-locking methods have yielded a significant reduction of decoherence. The quantitative investigation of qubit decoherence in the case of free and driven evolutions will be reported elsewhere.

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[9] O. Buisson et al. (to be published).